

Lesson 8-3

Example 1 Scientific to Standard Notation

Express each number in standard notation.

a. 1×10^6

$1 \times 10^6 = 1,000,000$ $n = 6$; move decimal point 6 places to the right.

b. 6.31×10^{-3}

$6.31 \times 10^{-3} = 0.00631$ $n = -3$; move decimal point 3 places to the left.

Example 2 Standard to Scientific Notation

Express each number in scientific notation.

a. **0.000501**

$0.000501 \rightarrow 00005.01 \times 10^n$ Move decimal point 4 places to the right.

$0.000501 = 5.01 \times 10^{-4}$ $a = 5.01$ and $n = -4$

b. **162.1**

$162.1 \rightarrow 1.621 \times 10^n$ Move decimal point 2 places to the left.

$162.1 = 1.621 \times 10^2$ $a = 1.621$ and $n = 2$

Example 3 Use Scientific Notation

The table shows the U.S. surplus or deficit in millions for 1995 through 2001.

Year	1996	1997	1998	1999	2000	2001
Surplus or Deficit(-)	-\$107,331	-\$21,957	\$70,039	\$124,360	\$236,993	\$121,000

Source: The World Almanac

a. Express the surplus or deficit for 1996, 1998 and 2000 in standard notation.

1996: $-\$107,331$ million = $-\$107,331,000,000$

1998: $\$70,039$ million = $\$70,039,000,000$

2000: $\$236,993$ million = $\$236,993,000,000$

b. Express the surplus or deficit for 1996, 1998 and 2000 in scientific notation.

1996: $-\$107,331,000,000 = -\1.07331×10^{11}

1998: $\$70,039,000,000 = \7.0039×10^{10}

2000: $\$236,993,000,000 = \2.36993×10^{11}

Example 4 Multiplication with Scientific Notation

Evaluate $(4.1 \times 10^{-5})(8.2 \times 10^{-2})$. Express the result in scientific and standard notation.

$$\begin{aligned}(4.1 \times 10^{-5})(8.2 \times 10^{-2}) &= (4.1 \times 10^{-5})(8.2 \times 10^{-2}) && \text{Commutative and Associative Properties} \\ &= 33.62 \times 10^{-7} && \text{Product of Powers} \\ &= (3.362 \times 10^1) \times 10^{-7} && 33.62 = 3.362 \times 10^1 \\ &= 3.362 \times (10^1 \times 10^{-7}) && \text{Associative Property} \\ &= 3.362 \times 10^{-6} \text{ or } 0.000003362 && \text{Product of Powers}\end{aligned}$$

Example 5 Division with Scientific Notation

Evaluate $\frac{5.612 \times 10^{-7}}{3.68 \times 10^{-6}}$. Express the result in scientific and standard notation.

$$\begin{aligned}\frac{5.612 \times 10^{-7}}{3.68 \times 10^{-6}} &= \left(\frac{5.612}{3.68} \right) \left(\frac{10^{-7}}{10^{-6}} \right) && \text{Associative Property} \\ &= 1.525 \times 10^{-1} \text{ or } 0.1525 && \text{Quotient of Powers}\end{aligned}$$